Question

A wheel of radius a and centre C rolls along a horizontal straight line without slipping. Find the parametric equation for the locus of a fixed point P on a spoke of the wheel at distance b from its centre. Take the x axis as the line through a low point of the curve and the parameter t as the angle PCA, where A is the point of contact of the wheel during the rolling.

Answer



We know: the arc QL = at so OL = at and $PM = b \sin t$ and $CM = b \cos t$ So the coordinates of P are

$$x = at - b\sin t$$
$$y = a - b\cos t$$