Question

Show that any simple function is measurable.

Answer

Let $f = \sum_{i=1}^{n} c_i X_{Ei}$

Then $\{x | f(x) \geq k\} = \bigcup_{c_i \geq k} Ei$ which is measurable.