## Vector Calculus Grad, Div and Curl

## Question

Calculate  $\mathbf{div}\mathbf{F}$  and  $\mathbf{curl}\mathbf{F}$  for the vector field

$$\underline{F} = x\underline{i} + x\underline{k}$$

Answer

$$\operatorname{div}\underline{F} = \frac{\partial}{\partial x}(x) + \frac{\partial}{\partial y}(0) + \frac{\partial}{\partial z}(x) = 1$$

$$\operatorname{curl}\underline{F} = \begin{vmatrix} \frac{i}{\partial} & \frac{j}{\partial x} & \frac{\underline{k}}{\partial y} \\ \frac{\partial}{\partial x} & \frac{\partial}{\partial y} & \frac{\partial}{\partial z} \\ x & 0 & x \end{vmatrix} = -\underline{j}$$